

Computer Graphics

Lecture-00

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Primary Focus

Develop thinking ability.

- problem solving skills.
- formal thinking.

Goals

- Be very familiar with a collection of *Computer Graphics algorithms*.
- Be intimately familiar with mathematics for Computer Graphics
- Be able to *apply* techniques in practical problems.

Textbook & References

- *Schaum's outlines series, THEORY AND PROBLEM OF COMPUTER GRAPHICS ,Second Edition, McGraw Hill.*

Computer Graphics

Chapter 3

Scan Conversion

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Scan Conversion

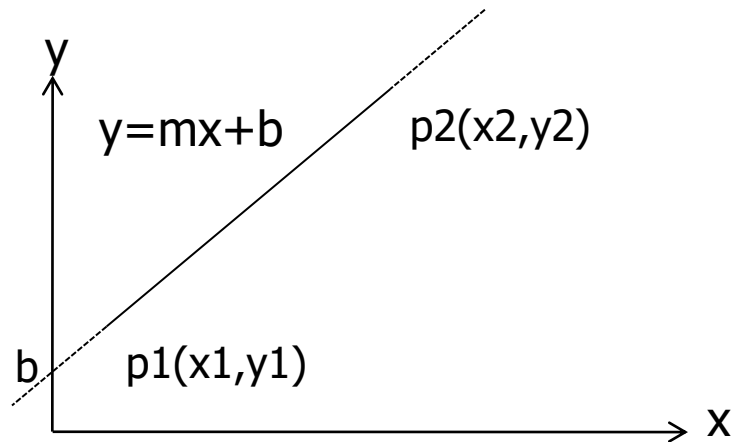
- Graphics System convert
 - each primitive(points ,lines, circles, ellipses etc.) from its geometric definition into a set of pixels that make up the picture in the image space.
 - This Conversion task is referred to as Scan Conversion.

Scan Converting a point

- (x, y) where x and y are real numbers within an image area.
- Need to be scan converted at pixel location (x', y')

Scan Converting a line

- Line drawing is accomplished by calculating intermediate positions along the line path between two specified end points.
- It is defined by the line equation $y=mx+b$, m is slope and b the y intercept of the line.
- Two end points are $p1(x1,y1)$ and $p2(x2,y2)$
- Line equation describes the coordinates of all the points that lie between the two end points.



Direct use of the Line Equation

- Scan convert p1 and p2 to pixel coordinates (x'_1, y'_1) and (x'_2, y'_2) then set $m = (y'_2 - y'_1)/(x'_2 - x'_1)$ and $b = y'_1 - mx'_1$.
- If $|m| \leq 1$, then for every integer value of x between and excluding x'_1 and x'_2 , calculate the corresponding value of y using the equation and scan convert (x,y).
- If $|m| \geq 1$, then for every integer value of x between and excluding y'_1 and y'_2 , calculate the corresponding value of x using the equation and scan convert (x,y).

DDA Algorithm

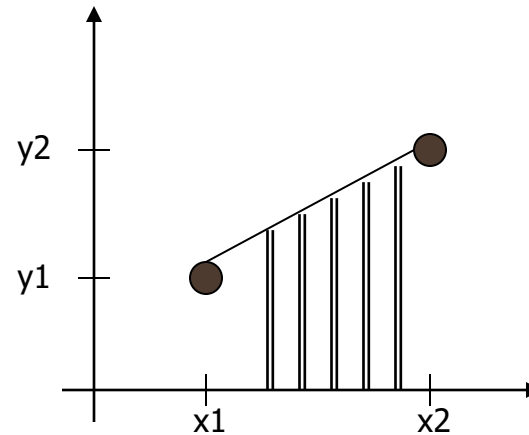
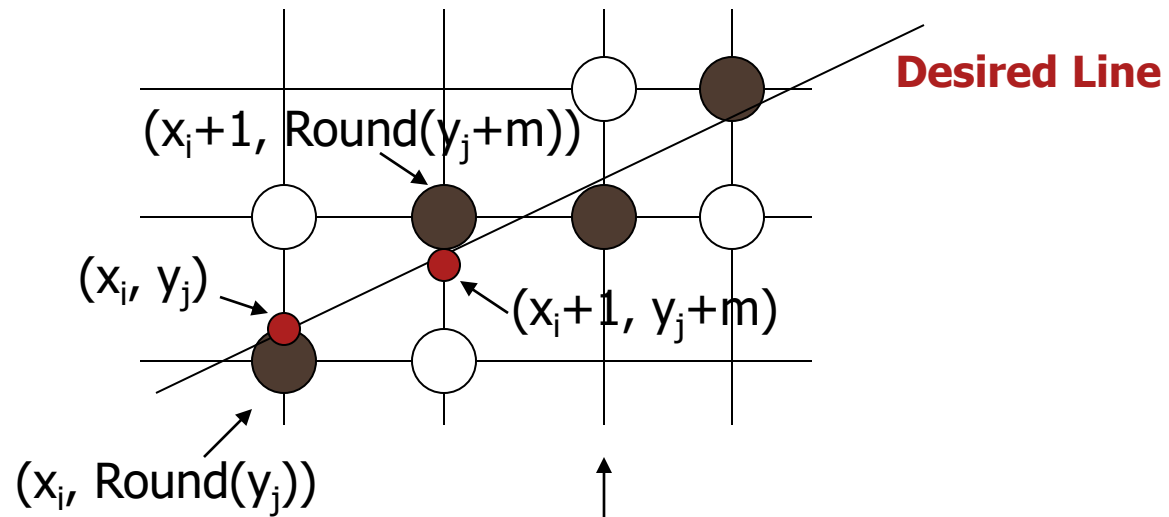
- *The digital differential analyzer (DDA) is an incremental scan-conversion method.*
- *Characterized by Performing calculations at each step using results from the preceding step.*
- *At each step i calculate (x_i, y_i) point on the line.*
- *Next point (x_{i+1}, y_{i+1})*
- *$\Delta y / \Delta x = m$, where $\Delta y = y_{i+1} - y_i$ and $\Delta x = x_{i+1} - x_i$, We have*

$$y_{i+1} = y_i + m\Delta x$$

or

$$x_{i+1} = x_i + \Delta y / m$$

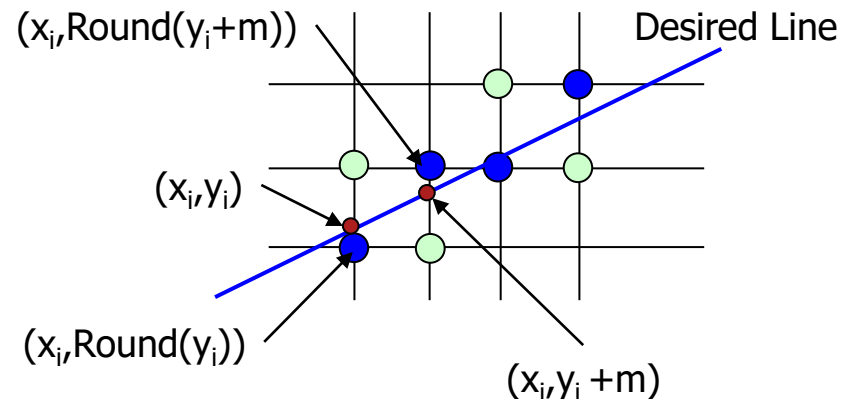
DDA Algorithm



DDA Algorithm

- DDA (“Digital Differential Analyzer”)
- Assume $0 \leq m \leq 1$.

$$\begin{aligned}
 y_{i+1} &= mx_{i+1} + B \\
 &= m(x_i + \Delta x) + B \\
 &= y_i + m\Delta x \\
 y_{i+1} &= y_i + m \quad [\Delta x = 1]
 \end{aligned}$$



```

void Line(int x0, int y0, int x1, int y1, int value) {
    double y = y0;
    double m = (y1 - y0) / (x1 - x0);    // 0 <= m <= 1
    for (int x = x0; x <= x1; x++) {
        WritePixel(x, Round(y), value);
        y += m;
    }
}
    
```

Require to eliminate floating point operations & variables

DDA ALGORITHM

- *DDA* algorithm is faster than the direct use of the line equation since it calculates points on the line without any floating point multiplication
- Cumulative error occurs.