# DAFFODIL INSTITUTE OF IT (DIIT) <br> BBA (Honours) in Tourism and Hospitality Management (THM) <br> Third Year Sixth Semester <br> Fundamentals of Finance <br> Chapter- 3 <br> Time Value of Money and its Application (Math) 

## Problem-5

Find the future value of the following investment:
The interest rate is $8 \%$ percent per year compounded annually. Tk 100 is invested each year beginning one year from now and continuing through year 10 . The proceeds are to be withdrawn in year 10 .

Solution: Given,

$$
\begin{aligned}
& \mathrm{R}=0.08 \\
& \mathrm{~A}=100 \\
& \mathrm{n}=10 \mathrm{yrs} . \\
& \mathrm{FV}=?
\end{aligned}
$$

We know,

$$
\begin{aligned}
& \mathrm{FV}=\frac{A\left\{(1+R)^{n}-1\right\}}{R} \\
& \mathrm{FV}=\frac{100\left\{(1+0.08)^{10}-1\right\}}{0.08} \\
& \mathrm{FV}=1448.65 \text { Ans. }
\end{aligned}
$$

## Problem-6

What is the present value of the following cash-flows at an interest rate of 12 percent per year: Tk 100 received each year beginning one year from now and ending 10 years from now.

Solution: Given,

$$
\begin{gathered}
\mathrm{R}=0.12 \\
\mathrm{~A}=100 \\
\mathrm{n}=10 \mathrm{yrs} . \\
\mathrm{PV}=?
\end{gathered}
$$

We know,

$$
\begin{aligned}
& \mathrm{PVa}=\mathrm{A}\left[\frac{1}{\mathrm{R}}-\frac{1}{\mathrm{R}(1+\mathrm{R})^{\mathrm{n}}}\right] \\
& \mathrm{PVa}=100\left[\frac{1}{.12}-\frac{1}{.12(1+.12)^{10}}\right] \\
& \mathrm{PV}=565 \text { Ans. }
\end{aligned}
$$

## Problem-7

If you wish to have Tk 10,000 ten years from now, how much money must you invest today in a saving certificate that pays 8 percent per year?

Solution: Given,

$$
\begin{gathered}
\mathrm{FV}=10,000 \\
\mathrm{n}=10 \mathrm{yrs} \\
\mathrm{R}=0.08
\end{gathered}
$$

Requirement: Present Value $(\mathrm{PV})=$ ?

$$
\begin{aligned}
& P V=F V \div(1+\mathrm{R})^{\mathrm{n}} \\
& \mathrm{PV}=10000 \div(1+0.08)^{10} \\
& \therefore \mathrm{PV}=4,632 \text { Ans. }
\end{aligned}
$$

## Problem-8

BTI has been doing real estate business for last 20 years, you have selected an apartment of BTI at Green Road costing Tk 25 lakh. You have three alternative offers:
(i) Pay full in cash.
(ii) Pay $25 \%$ of the cost in cash immediately and pay Tk 2.25 lakh in each instalment tor next ten years.
(iii) Pay $40 \%$ of the cost in cash and take a loan of Tk 15 lakh from HBFC at $15 \%$ interest to be paid in equal monthly instalment over a next 20 years.

Which offer should you accept if opportunity cost is $12 \%$.
Solution: Given,

$$
\begin{gathered}
\mathrm{N}=20 \mathrm{yrs} . \\
\mathrm{PV}=25,00,000 \\
\mathrm{R}=0.12
\end{gathered}
$$

Requirement: Present Value (PV) =?
Alternative (i): Present Value $(P V)=25,00,000$

Alternative (ii): $\mathrm{PV}=$ Cash down payment $+\mathrm{A}\left[\frac{1}{\mathrm{R}}-\frac{1}{\mathrm{R}(1+\mathrm{R})^{\mathrm{n}}}\right]$

$$
\begin{aligned}
& =2500000 \times 25 \%+2,25,000\left[\frac{1}{0.12}-\frac{1}{0.12(1+0.12)^{10}}\right] \\
& =6,25,000+1271300 \\
& =18,96,300
\end{aligned}
$$

Alternative (iii): Alternative (ii): $\mathrm{PV}=$ Cash down payment $+\mathrm{A}\left[\frac{1}{\mathrm{R}}-\frac{1}{\mathrm{R}(1+\mathrm{R})^{\mathrm{n}}}\right]$

$$
\begin{aligned}
& =2500000 \times 40 \%+19,752\left[\frac{1}{0.12 \div 12}-\frac{1}{0.12 \div 12(1+0.12 \div 12)^{20 \times 12}}\right] \\
& =1000000+19752\left[\frac{1}{0.01}-\frac{1}{0.01(1+0.01)^{240}}\right] \\
& =10,00,000+17,93,865 \\
& \quad=27,93,865
\end{aligned}
$$

Note: Here, the instalment for HBFC will be as under:

$$
\begin{aligned}
& \mathrm{PV}=\mathrm{A}\left[\frac{1}{\mathrm{R}}-\frac{1}{\mathrm{R}(1+\mathrm{R})^{\mathrm{n}}}\right] \\
\Rightarrow & 15,00,000=\mathrm{A}\left[\frac{1}{0.15 \div 12}-\frac{1}{0.15 \div 12(1+0.15 \div 12)^{20 \times 12}}\right] \\
\Rightarrow & 15,00,000=\mathrm{A}\left[\frac{1}{0.0125}-\frac{1}{0.0125(1+0.0125)^{240}}\right] \\
\Rightarrow & 1500000=\mathrm{A}(75.9423) \\
\Rightarrow & \mathrm{A}(75.9423)=1500000 \\
\Rightarrow & \mathrm{~A}=1500000 \div(75.9423) \\
& \therefore \mathrm{A}=19752
\end{aligned}
$$

Decision: Since alternative (ii) has the lowest PV (cost), so it should be accepted.

## Problem- 9

Mr. Zahid plans to send his son for higher studies abroad after 10 years. He expects the cost of these studies to be Tk $10,00,000$. How much should he save annually to have a sum of $\mathrm{Tk} 10,00,000$ at the end of 10 years, if the interest rate is 12 percent?

Solution: Given,

$$
F V=10,00,000
$$

$$
\begin{aligned}
& \mathrm{n}=10 \mathrm{yrs} . \\
& \mathrm{R}=0.12 \\
& (\mathrm{~A})=?
\end{aligned}
$$

We know,

$$
\begin{aligned}
& \mathrm{FVa}=\frac{A\left\{(1+R)^{n}-1\right\}}{R} \\
\Rightarrow & 1000000=\frac{A\left\{(1+.12)^{10}-1\right\}}{.12} \\
\Rightarrow & 1000000==\frac{A\{2.1058\}}{.12} \\
\Rightarrow & 1000000=\mathrm{A}(17.5487) \\
\Rightarrow & \mathrm{A}(17.5487)=1000000 \\
= & \mathrm{A}(17.5487)=1000000 \div 17.5487 \\
\therefore & \mathrm{~A}=56984.1641 \mathrm{Ans} .
\end{aligned}
$$

